

## Appendix B Formula Summary

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**Frequency:** midpoints - proportion,  $p$  - percentage - percentile - mean from frequency distribution - **Central Tendency:** mean - median - mode - **Variability** - range - sum of deviations - sum of square - range - variance - standard deviation - quartiles - interquartile - semi-interquartile range - **Standard Score** - z-scores - other standard scores - percentile - percent rank - **Normal Curve** - area under curve - NCE - Correlation - sum of products - covariance, Pearson  $r$  - standard error of  $r$  - confidence interval of  $r$  - Spearman  $r$

### Frequency

Midpoint =  $\frac{U_a - L_a}{2}$ , where  $U_a$  is the upper apparent limit and  $L_a$  is the lower

$N = \sum f$ , where  $f$  is the frequency of each group, and  $N$  is total frequency

proportion =  $p = \frac{f}{N}$ , where  $f$  is the frequency, and  $N$  is total frequency

percentage =  $p(100) = \frac{f}{N}(100)$ , where  $f$  is the frequency, and  $N$  is sum of frequencies

$$P\% = LL_i + \left[ \left( \frac{n_p - C_f}{f_i} \right) \cdot I \right]$$

where  $P\%$  = any specified percentile point

$LL_i$  = the *exact lower limit* or *real lower limit* of the group interval containing the percentile point,  $P\%$

$n_p$  = number of scores or cases comprising the specified percentage for  $n$ .

$C_f$  = cumulative frequency up to but not including the percentile interval

$f_i$  = frequency within the percentile interval

$I$  = group interval size or class size

Mean from frequency:

mean =  $\bar{X} = \frac{\sum f_i X_i}{n}$ , where  $\sum f_i X_i$  is product of frequency and score or midpoint

**Central Tendency**

Population mean:  $\mu = \frac{\sum X}{N}$ , where  $\sum X$  is sum of scores, and  $N$  is population size

Sample:  $\bar{X} = M = \frac{\sum X}{n}$ , where  $\sum X$  is sum of scores, and  $n$  is sample size

Median: (a) **odd**  $N$ , median = middle score of an ordered set (min to max)

(b) **even**  $N$ , median =  $\frac{\text{two center scores}}{2}$ , average of center scores

Mode: the most frequent score(s) from a simple frequency distribution

**Variability**

Range =  $X_{\max} - X_{\min}$ , where  $X_{\max}$  is maximum score, and  $X_{\min}$  is minimum score

Sum of deviation from mean:  $\sum(X - \bar{X}) = 0$ , where  $\bar{X}$  is mean

Sum of square:  $SS = \sum(X - M)^2$  or  $SS = \sum(X - \bar{X})^2$  (definition formula)

$$SS = \sum X^2 - \frac{(\sum X)^2}{N} \text{ (computational formula)}$$

Population Variance =  $\sigma^2$  (Sigma squared) =  $\frac{\sum(X - \bar{X})^2}{N}$  (definition)

$$\sigma^2 = \frac{SS}{N} = \frac{\sum X^2 - \frac{(\sum X)^2}{N}}{N} \text{ (computational)}$$

Sample Variance =  $s^2 = \frac{\sum(X - \bar{X})^2}{n - 1}$  (definition)

$$s^2 = \frac{SS}{n - 1} \text{ (computational, see SS above)}$$

standard deviation =  $\sigma$  or  $s = \sqrt{\text{variance}} = \sqrt{\sigma^2} = \sqrt{s^2}$

Population standard deviation =  $\sigma$  (Sigma) =  $\sqrt{\frac{\sum(X - \bar{X})^2}{N}}$  (definition)

$$\sigma = \sqrt{\sigma^2} = \sqrt{\frac{SS}{N}} = \sqrt{\frac{\sum X^2 - \frac{(\sum X)^2}{N}}{N}} \text{ (computational)}$$

$$\text{Sample Variance} = s = \sqrt{\frac{\sum(X - \bar{X})^2}{n - 1}} \quad (\text{definition})$$

Degrees of freedom, *df*, for sample variance:  $df = n - 1$

$$s = \sqrt{s^2} = \sqrt{\frac{SS}{n - 1}} = \sqrt{\frac{SS}{df}} = \sqrt{\frac{\sum X^2 - \frac{(\sum X)^2}{n}}{n - 1}} \quad (\text{computational})$$

50% Quartile:  $Q_2 = \text{Median}$  (50% of scores at or below median)

25% Quartile:  $Q_1 = \text{Median}$  of first half of dataset (25% of scores at or below  $Q_1$ )

75% Quartile:  $Q_3 = \text{Median}$  of second half of dataset (25% of scores at or above  $Q_3$ )

interquartile range:  $IQR = Q_3 - Q_1$

$$\text{semi-interquartile range} = \frac{Q_3 - Q_1}{2}$$

**Standard Score**

$$z = \frac{X - \mu}{\sigma} \quad \text{or} \quad z = \frac{X - M}{s} \quad (\text{sample, } M \text{ is mean})$$

50% Quartile:  $Q_{50} = \text{Median}$  (50% of scores at or below median)

Other Standard Scores:

Other Standard Score Systems		
standard score = $z = \frac{X - \mu}{\sigma}$		
Standard Score System	$\mu$	$\sigma$
z scores	0	1
T score	50	10
General Aptitude Test Battery (GATB)	100	20
College Entrance Examination Board (CEEB)	500	100
IQ Test	100	16

Percentile,  $P_{\%}$  raw score,  $X = \sigma(z) + \mu$

Example:  $P_{75}$  is  $X = 87.39$  [given  $\sigma = 2.5$  and  $\mu = 85.7$ ;  $z = 0.675$  for  $\Pr(\leq 0.75)$ ]

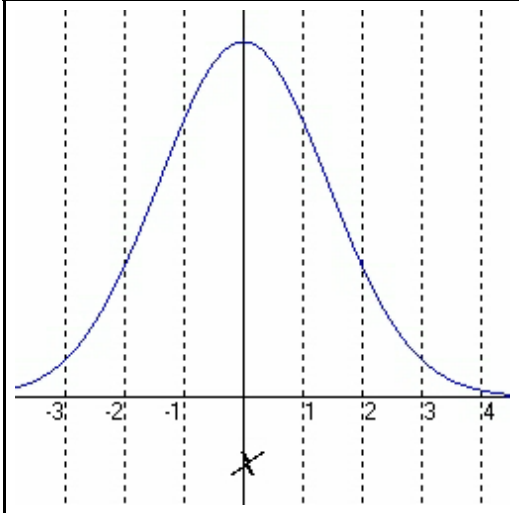
The raw score that 75% of distribution is below: 75 percentile

Percent Rank, the percentile of a given raw score

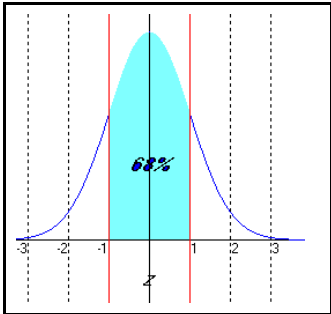
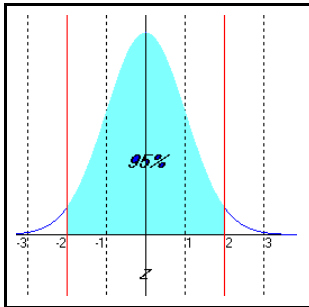
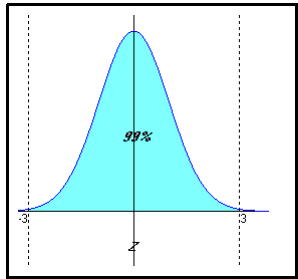
Example:  $Pr_{89}$  (percent rank of 89),  $X = 89$  ( $\sigma = 2.5$  and  $\mu = 85.7$ ;  $z = 1.32$ )

$\Pr(z \leq 1.32) = 90.66$  or  $Pr_{89} = 90.66\%$

### Normal Curve

<p>Normal Curve formula</p> $y = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{x-\mu^2}{2\sigma^2}}$ <p> <math>y</math> = height of normal curve  <math>\sigma</math> = standard deviation  <math>\pi</math> = pi, or about 3.14  <math>e</math> = natural logarithm constant, about 2.718  <math>X</math> = any score  <math>\mu</math> = population mean                 </p>	<p>Normal Curve Graph</p> 
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### Area under curve between various z-scores

<p>Pr between <math>z = -1</math> and <math>+1</math></p> 	<p>Pr between <math>z = -2</math> and <math>+2</math></p> 	<p>Pr between <math>z = -3</math> and <math>+3</math></p> 
<p>Area = 68% between <math>z = -1</math> &amp; <math>+1</math></p>	<p>Area = 95% between <math>z = -2</math> &amp; <math>+2</math></p>	<p>Area = 99% between <math>z = -3</math> &amp; <math>+3</math></p>

Normal Curve Equivalence (NCE)

$$NCE = 21z + 50$$

## Correlation

Sum of square of X:  $SS_x = \sum(X - M_x)^2$  or  $SS_x = \sum(X - \bar{X})^2$  (definition formula)

Sum of square of Y:  $SS_y = \sum(Y - M_y)^2$  or  $SS_y = \sum(Y - \bar{Y})^2$  (definition formula)

Sum of products:  $SP = \sum[(X - M_x)(Y - M_y)]$  (definition formula)

$$SP = \sum XY - \frac{(\sum X)(\sum Y)}{n} \text{ (computational formula)}$$

$$\text{Covariance, } S_{xy} = \frac{\sum[(X - M_x)(Y - M_y)]}{n - 1}$$

$$\text{Pearson correlation coefficient, } r_{xy} = \frac{S_{xy}}{S_x S_y} = \frac{SP}{\sqrt{SS_x SS_y}}$$

where  $S_{xy}$  is covariance,  $S_x$  and  $S_y$  are standard deviations of X & Y  
 $SS_x$  and  $SS_y$  are sum of square of X and Y

$$\text{Pearson } r = \frac{N \sum XY - (\sum X)(\sum Y)}{\sqrt{N \sum X^2 - (\sum X)^2} \cdot \sqrt{N \sum Y^2 - (\sum Y)^2}} \text{ (computational formula)}$$

standard error of  $r$

$$s_r = \frac{1}{\sqrt{n - 1}} \text{ (estimate of standard deviation of } r)$$

Confidence interval for  $r$

95% of all sample  $r$ 's fall between  $0 \pm 1.96s_r$

99% of all sample  $r$ 's fall between  $0 \pm 2.58s_r$

Spearman correlation coefficient,  $r_s$

Spearman rank-Difference Method

$$r_s = 1 - \frac{6 \sum D^2}{n(n^2 - 1)}$$

where  $r_s$  is correlation (population symbol is  $\rho$  or  $\rho$ ),  $\sum D^2$  is sum of square difference between ranks, and  $n$  is number of pairs of ranks