

# Linear Regression

## Significance of Regression Equation

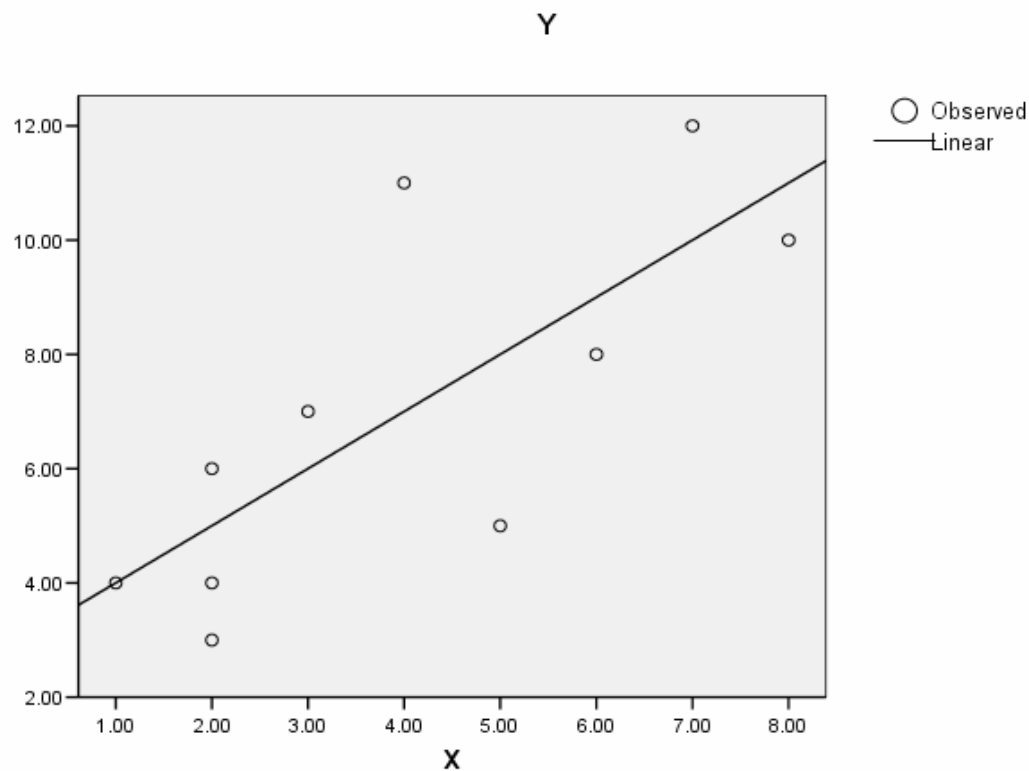
Course: Statistics 1

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# Regression Model

$$Y = 1.368X + 3.35$$



<b><i>X</i></b> <b><i>Independent</i></b>	<b><i>Y</i></b> <b><i>Dependent</i></b>
4	11
3	7
1	4
7	12
2	6

# Significance of Regression Equation

- The significance of Pearson correlation can be used to test the significance of the regression equation (when single X)
- $H_0$ : There is no relationship between X and Y **or**
- $H_0$ : The regression equation does not account for a significant portion of the variance of Y scores
- Process of testing significance of a regression equation is called analysis of regression and similar to analysis of variance (ANOVA)

# Sums of Squares of Regression

$$\text{std error of est} = \sqrt{\frac{SS_{Res}}{df}} = \sqrt{\frac{6.33}{3}} = 1.45$$

$$SS_{Reg} = r^2 SS_Y = (0.929)^2(46) = 39.70$$

$$SS_{Res} = (1 - r^2)SS_Y = [1 - (0.929)^2](46) = 6.30$$

$$r = \frac{SP}{\sqrt{SS_X SS_Y}} = \frac{29}{\sqrt{21.2(46)}} = 0.929 \text{ and } r^2 = 0.863$$

# Analysis of Regression

- The regression analysis uses an  $F$ -ratio to determine the amount of variance accounted for by the regression equation
- $F$ -ratio:  $MSR/MSE$  (MS is mean square)
  - MSR is  $MS_{\text{Reg}}$  or variance predicted by regression equation
  - MSE is  $MS_{\text{Res}}$  or unpredicted variance due to chance or other than regression equation

# Analysis of Regression Table

Source	SS	<i>df</i>	<i>MS</i>	<i>F</i>
Regression	SSReg	1	MSR = SSReg/1	MSR/MSE
Residual	SSRes	$n - 2$	MSE = SSRes/( $n-2$ )	
Total	Sum SS	Sum <i>df</i>		

# Mean Square Calculations

$$MS_{\text{Reg}} = \frac{SS_{\text{regression}}}{df_{\text{reg}}} = \frac{39.67}{1} = 39.67$$

$$MS_{\text{Res}} = \frac{SS_{\text{residual}}}{df_{\text{res}}} = \frac{SS_{\text{residual}}}{n-2} = \frac{6.33}{3} = 2.11$$

$$F\text{-ratio} = F = \frac{MS_{\text{regression}}}{MS_{\text{residual}}} = \frac{39.67}{2.11} = 18.80$$

# ANOVA: Regression Table

Source	SS	df	MS	F
Regression	39.67	1	MSR = 39.67	MSR/MSE = <b>18.80</b>
Residual	6.33	3	MSE = 2.11	
Total	46	4		



# Conclusion

- $F_{cv} = 10.13$   
 $df = 1, 3$ , and  $\alpha = 0.05$
- $F_{stat} > F_{cv}$  or  $18.80 > 10.13$
- **Reject**  $H_0$  that the regression equation does not accounts for a significant portion of the variability for the Y scores
- **Conclude** that regression equation is a **good model**
- Pearson  $r$  is **0.93**, high

<b>df2</b>	<b>df = 1</b>	<b>df = 2</b>
1	161.45	199.50
2	18.51	19.00
3	<b>10.13</b>	9.55
4	7.71	6.94
5	6.61	5.79

# SPSS Output: ANOVA

ANOVA<sup>b</sup>

Model		Sum of Squares	df	Mean Square	F	Sig.
1	Regression	39.670	1	39.670	18.800	.023 <sup>a</sup>
	Residual	6.330	3	2.110		
	Total	46.000	4			

a. Predictors: (Constant), X

b. Dependent Variable: Y

# SPSS Output: Regression Model

Coefficients<sup>a</sup>

Model		Unstandardized Coefficients		Standardized Coefficients	t	Sig.
		B	Std. Error	Beta		
1	(Constant)	3.349	1.254		2.671	.076
	X	1.368	.315	.929	4.336	.023

a. Dependent Variable: Y